

# **Agent-Based Computational Economics**

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## **A Constructive Approach to Economic Theory**

Presenter (Spring 2005):

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# Basic References

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- ★ Leigh Tesfatsion, **“Agent-Based Computational Economics: A Constructive Approach to Economic Theory”**

Chapter 1 in Leigh Tesfatsion and Kenneth L. Judd, Editors, *Handbook of Computational Economics, Volume 2: Agent-Based Computational Economics*, Handbooks in Economics Series, North-Holland, Amsterdam, to appear.

**<http://www.econ.iastate.edu/tesfatsi/hbace.htm>**

- ★ **ACE Website**

**<http://www.econ.iastate.edu/tesfatsi/ace.htm>**

# Outline

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- ★ The Complexity of Decentralized Market Economies
- ★ What is Agent-Based Computational Economics (ACE)?
- ★ An Illustrative ACE Model of a Decentralized Market Economy
- ★ Computational Laboratory Implementation (joint work with C. Cook)

# The Complexity of Decentralized Market Economies

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- ◆ Large numbers of economic agents involved in *distributed local interactions*
- ◆ *Two-way feedback* between microstructure and macro regularities mediated by agent interactions
- ◆ Potential for *strategic behaviour*
- ◆ Pervasive *behavioural uncertainty*
- ◆ Possible existence of *multiple equilibria*
- ◆ Critical role of *institutional arrangements*

# What is Agent-Based Computational Economics (ACE)?

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- ◆ **Culture-dish approach** to the study of decentralized market processes
- ◆ **Experimental study** of economies computationally modeled as evolving systems of autonomous interacting agents with learning capabilities

- ◆ **ACE Website**

[www.econ.iastate.edu/tesfatsi/ace.htm](http://www.econ.iastate.edu/tesfatsi/ace.htm)

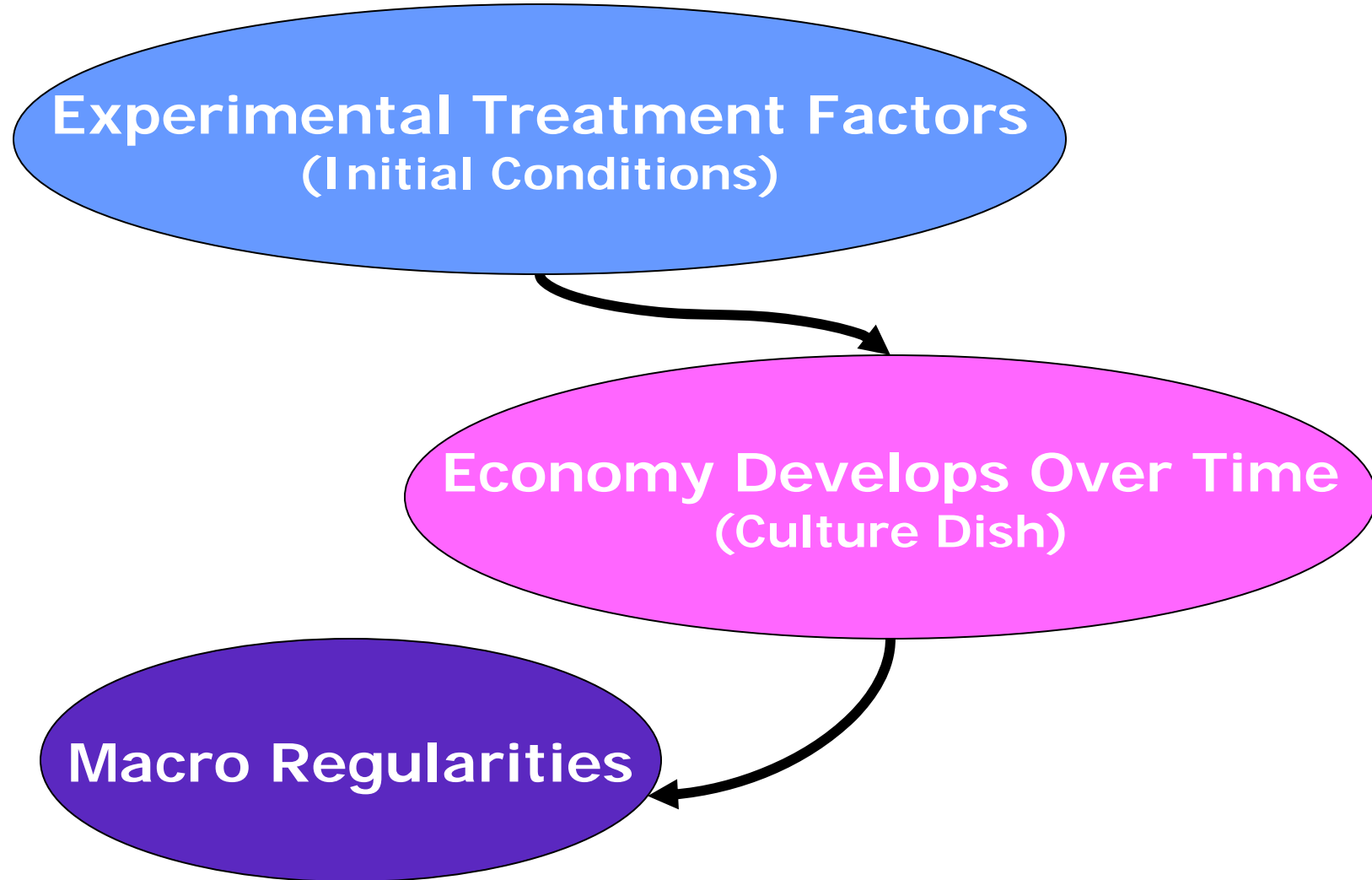
# ACE Modeling: Culture Dish Analogy

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- ◆ Modeler constructs a **virtual economic world** populated by various agent types (economic, social, biological, physical)
- ◆ Modeler sets **initial conditions**
- ◆ The world then **develops over time** without further outside intervention
- ◆ World driven solely by **agent interactions**

# ACE Modelling: Culture Dish Analogy

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# Key Characteristics of ACE Models

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- ◆ **Agents** are encapsulated software programs capable of
  - *Adaptation* to environmental conditions
  - *Social communication* with other agents
  - *Goal-directed learning*
  - *Autonomy* (self-activation and self-determinism based on private internal processes)
- ◆ Agents can be situated in **realistically rendered problem environments**
- ◆ **Behaviour/interaction patterns can evolve over time**

# Increased facility for modeling autonomous agents

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- ◆ *Distributed agent control*, not just distributed agent actions.
- ◆ Agents can decide for themselves which actions they perform, and when, based on *private internal processes*.
- ◆ *Implication*: Major source of uncertainty for agents in ACE models is not knowing what other agents will do (unpredictable endogenous heterogeneity!)

# TradeBot: A Virtual Trader

## Public Access:

### // **Public Methods**

Protocols governing communication with other traders;  
Protocols governing search for trade partners;  
Protocols governing the conduct of trades;  
Methods for receiving data (e.g., a “telephone”);  
Methods for retrieving Trader data.

## Private Access:

### // **Private Methods**

Methods for gathering, storing, and sending data;  
Method for calculating my expected utility assessments;  
Method for calculating my actual utility outcomes;  
Method for updating my trade strategy (**learning**);  
Methods for updating my methods (**learning to learn**).

### // **Private Data**

Data about myself (my history, utility fct., current wealth...);  
Data recorded about external world (rivals' bids/asks...);  
Addresses (e.g., a “telephone book”).

# ACE and Macro Regularities

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**Key Issue:** Is there a causal explanation for a **persistently observed macro regularity**?

## ACE Approach:

- ◆ Construct an *agent-based world* capturing salient aspects of the empirical situation.
- ◆ Investigate whether the observed macro regularity can be *reliably generated* “from the bottom up” in this agent-based world.
- ◆ **Generative Science** (Epstein/Axtell, 1996)

# ACE and Market Design

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**Key Issue:** Does a proposed or actual market design ensure **efficient, fair, and orderly market outcomes over time** despite repeated attempts by traders to game the design for their own personal advantage?

## ACE Approach:

- ◆ Construct an *agent-based world* capturing salient aspects of the market design.
- ◆ *Introduce self-interested traders with learning capabilities.* Let the world develop over time. Observe/evaluate resulting market outcomes.

# ACE and Qualitative Analysis

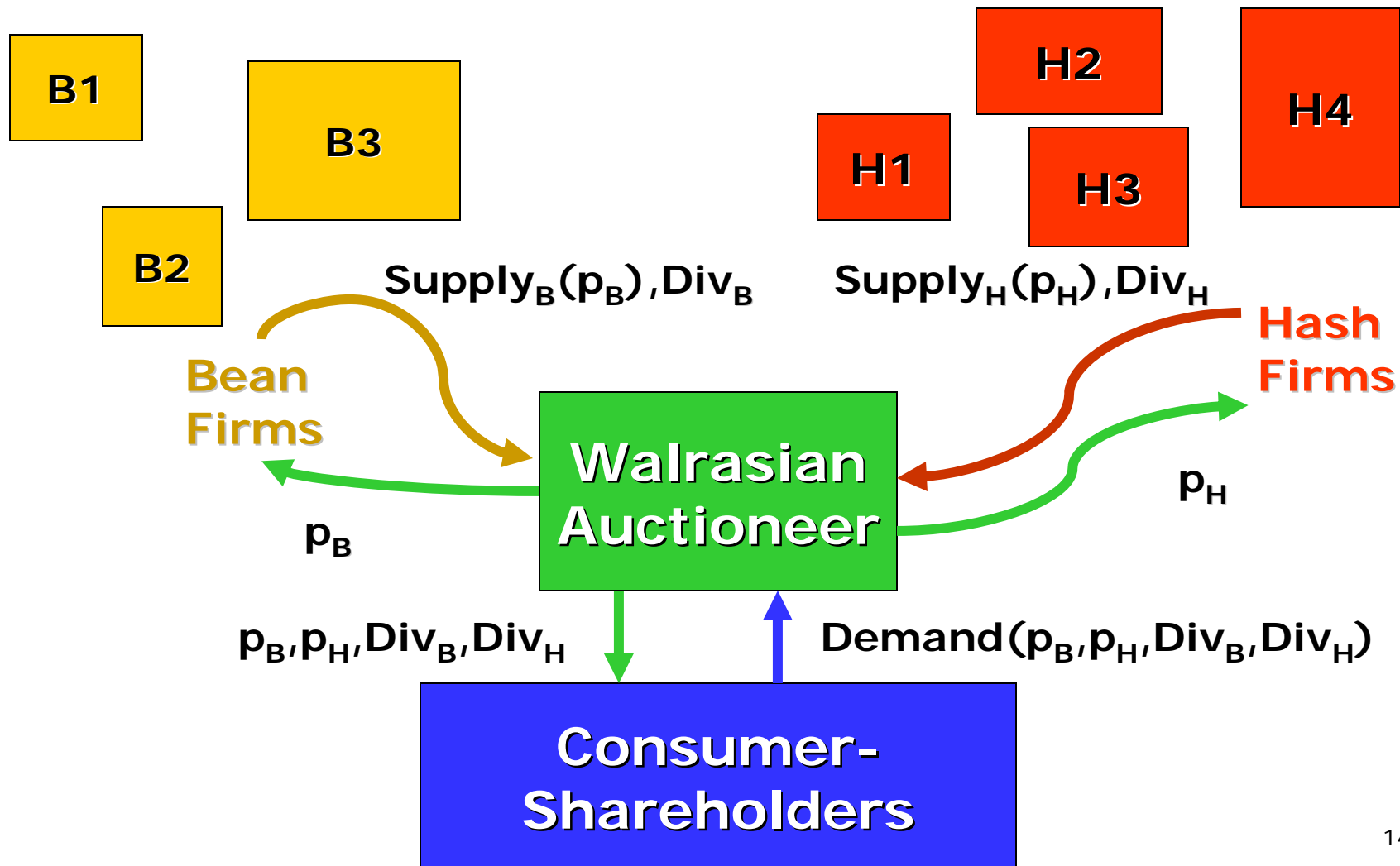
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## Key Issue: Constructive Understanding

**Example:** If you had to construct a profit-seeking firm capable of surviving and even prospering in a realistically rendered decentralized market economy, how would you go about it?

**Question:** If economists are not capable of rising to this constructive challenge, to what extent can we be said to have a *scientific* understanding of real-world decentralized market economies?

# Illustration: Start with a Traditional Walrasian Economy



# Plucking Out the Walrasian Auctioneer



Bean  
Firms

Hash Firms

Firm-Consumer  
Connections??

Consumer-  
Shareholders

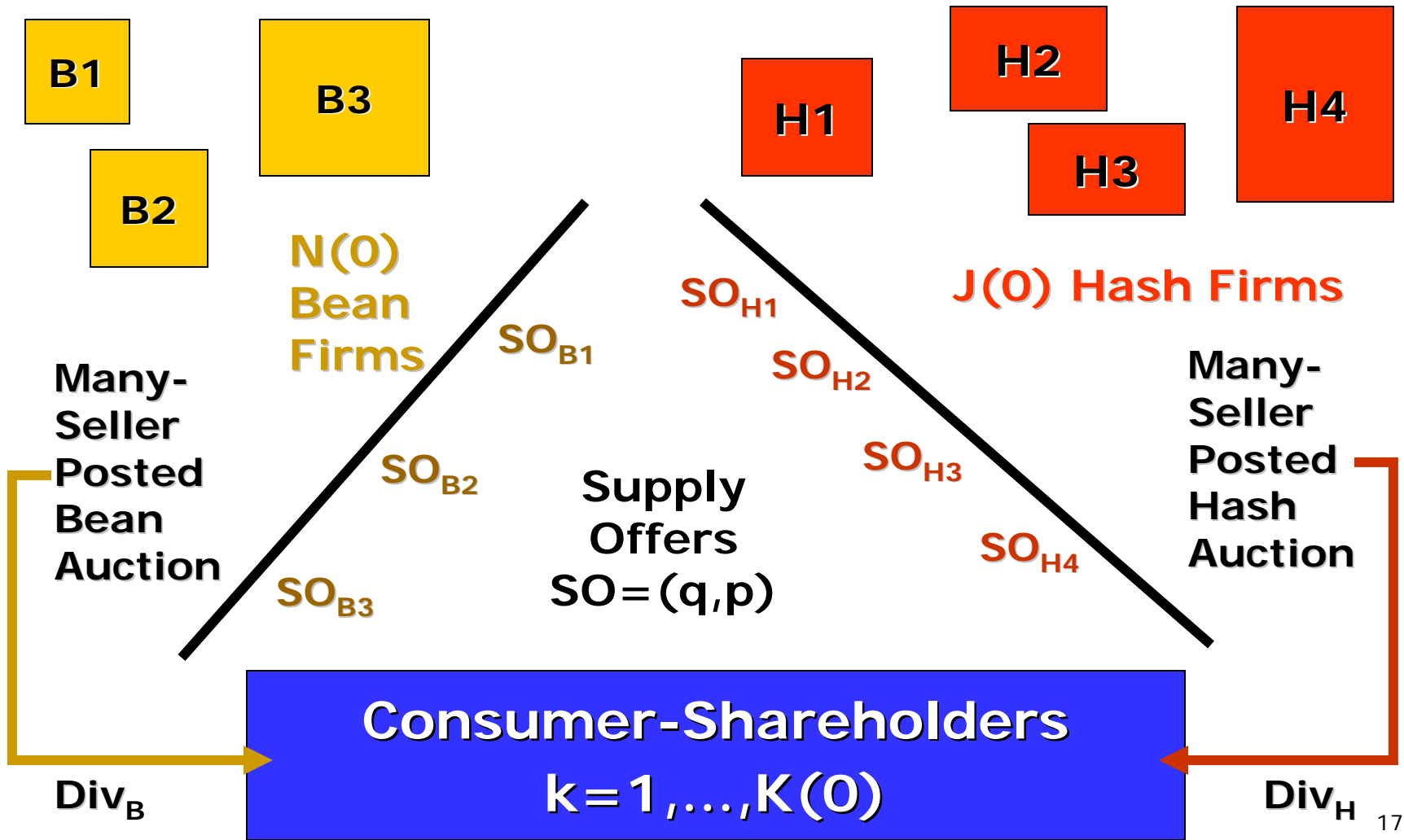
# Plucking Out the Walrasian Auctioneer

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Focus must now be **procurement processes**

- ◆ Deciding on production levels and unit prices
- ◆ Potential supplier/customer identification
- ◆ Submission of supply offers/demand bids
- ◆ Comparison/evaluation of opportunities
- ◆ Supplier/customer selection
- ◆ Negotiation among suppliers/customers
- ◆ Transaction and payment processing
- ◆ Managing supplier/customer relationships

# Example of an ACE Trading World



# ACE Firms

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- ◆ Each firm  $f$  starts out ( $T=0$ ) with *Money<sub>f</sub>(0)* and a production capacity *Cap<sub>f</sub>(0)*.
- ◆ Firm  $f$ 's *FixedCost<sub>f</sub>(0)* in each period  $T \geq 0$  is proportional to its current capacity.
- ◆ At beginning of each period  $T \geq 0$ , firm  $f$  posts a *SupplyOffer<sub>f</sub> = (production level, unit price)*
- ◆ At end of  $T \geq 0$ , firm  $f$  is **insolvent** if it has  $\text{NetWorth}_f(T) = [\text{Profit}_f(T) + M_f(T) + \text{ValCap}_f(T)] \leq 0$
- ◆ If **solvent**, firm  $f$  *allocates profits* (+ or -) between Money<sub>f</sub>, Cap<sub>f</sub>, and dividend payments.

# ACE Consumer-Shareholders

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- ◆ Each consumer  $k$  starts out ( $T=0$ ) with a *lifetime money endowment profile*  
(  $Money_{youth}$  ,  $Money_{middle}$  ,  $Money_{old}$  )
- ◆ Consumer  $k$  has a **utility function** of the form  
$$U_k(T) = (bean(T) - b_k^*) \cdot (hash(T) - h_k^*)^{\theta_k}$$
- ◆ In each  $T \geq 0$ , consumer  $k$  attempts to ensure her survival/happiness by *searching* for  $bean$  and  $hash$  to buy at *lowest possible prices*.
- ◆ At end of each  $T \geq 0$ , consumer  $k$  **dies** if she fails to consume at least  $(b_k^*, h_k^*)$ .

# Experimental Design Treatment Factors

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- ◆ **Initial size of consumer sector** [  $K(0)$  ]
- ◆ **Initial firm concentration** [  $N(0), J(0), Cap(0)$  ]
- ◆ **Learning** (supply offer/profit allocation decisions)
- ◆ **Firm cost functions**
- ◆ **Firm initial money holdings** [  $Money_f(0)$  ]
- ◆ **Firm rationing method** (for excess demand)
- ◆ **Consumer search process**
- ◆ **Consumer money endowment profiles**  
(rich, poor,  $\nearrow$ ,  $\searrow$ , life cycle u-shape)
- ◆ **Consumer preferences** ( $\theta$  values)
- ◆ **Consumer subsistence needs** ( $b^*, h^*$ )

# Interesting Issues to be Explored

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- ◆ Initial conditions → **Market efficiency**  
(Walrasian equilibrium benchmark)
- ◆ Initial conditions → **Market power**  
(Walrasian equilibrium benchmark)
- ◆ Initial conditions → **Carrying capacity**  
(Survival of firms/consumers in long run)
- ◆ **Standard concentration measures at T=0**  
(Good predictors of long-run market power?)
- ◆ Importance of **learning vs. market structure**  
for market performance (*Gode/Sunder, JPE, 1993*)

# Possible Structural Extensions

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- ◆ **Introduce Other Coordination Mechanisms:**  
Let traders engage in direct social communication (evolution of trust, implicit contracts, loyalty,...);  
Introduce retail stores, insurance companies,...
- ◆ **Co-Evolution of Behaviours and Institutions:**  
Let trading behaviours (supply offers, profit allocation rules) and institutional arrangements (market protocols, consumer search process,...) *co-evolve* together.
- ◆ **Demographics/Biological Reproduction:**  
Consumers can be modelled as having genotypes as well as phenotypes, permitting haploidy or diploidy reproduction (parent(s) → children)

# ACE Trading World: Implementation

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C. Cook and L. Tesfatsion, "**Agent-Based Computational Laboratories for the Experimental Study of Complex Economic Systems,**" Working Paper, ISU Department of Economics, *in progress*.

- ◆ Computational laboratory implementation
- ◆ Programming language C#/.Net (WinDesktops)
- ◆ Under development for Econ 308 (ACE course)  
[www.econ.iastate.edu/classes/econ308/tesfatsion/](http://www.econ.iastate.edu/classes/econ308/tesfatsion/)

# What is a Computational Laboratory?

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## ◆ *Computational framework*

for the study of complex system behaviors by means of controlled and replicable experiments

## ◆ *Graphical user interface (GUI)*

permits experimentation by users with no background in programming

## ◆ *Modular/extensible software support*

permits CL capabilities to be changed/extended by users who have programming skills

## ◆ **ACE Comp Lab Sites**

[www.econ.iastate.edu/tesfatsi/acedemos.htm](http://www.econ.iastate.edu/tesfatsi/acedemos.htm)

[www.econ.iastate.edu/tesfatsi/acomplab.htm](http://www.econ.iastate.edu/tesfatsi/acomplab.htm)

# Finished Example: The Trade Network Game (TNG) Lab

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- ◆ **Evolution of trade networks**  
among strategically interacting traders  
(buyers, sellers, dealers) with trades=PD games
- ◆ **Traders instantiated as “tradebots”**  
(autonomous software entities)
- ◆ **Event-driven communication**  
among traders to determine their trade partners
- ◆ **Tradebots evolve trade strategies**  
starting from *initially random* strategies
- \* <http://www.econ.iastate.edu/tesfatsi/tnghome.htm>




# TNG Results Screen

TNG Lab - C:\tng\fig3-7.tng

File Edit View Help

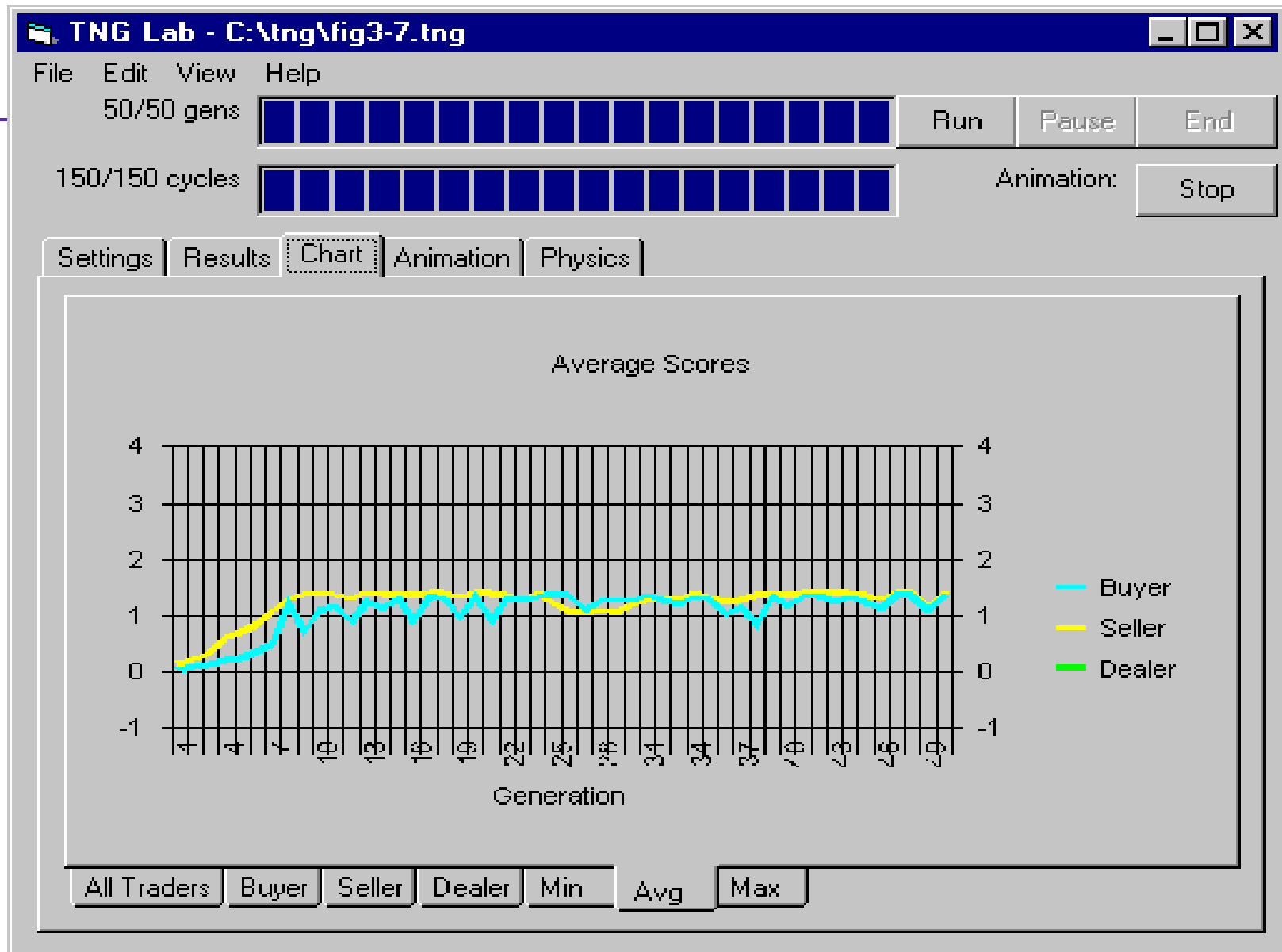
50/50 gens  Run Pause End

150/150 cycles  Animation: Stop

Settings Results Chart Animation Physics

Generation	Buyer Average	Buyer Minimum	Buyer Maximum	Buyer Std Dev	Seller Average	Seller Minimum
37	+1.1713	-0.1307	+1.3233	+0.3930	+1.2902	+0.2160
38	+0.8433	+0.7000	+0.9500	+0.0700	+1.3639	+0.9667
39	+1.3542	+1.3333	+1.3633	+0.0098	+1.4000	+1.4000
40	+1.1678	+0.7033	+1.2700	+0.1451	+1.3706	+1.0467
41	+1.3386	+1.2800	+1.3633	+0.0232	+1.4000	+1.4000
42	+1.3581	+1.3433	+1.3633	+0.0069	+1.4000	+1.4000
43	+1.2500	+1.1267	+1.2967	+0.0453	+1.3972	+1.3667
44	+1.3400	+1.3000	+1.3567	+0.0156	+1.4000	+1.4000
45	+1.2511	+0.6633	+1.3467	+0.1793	+1.3550	+0.8600
46	+1.1322	-0.1407	+1.2833	+0.3845	+1.3058	+0.3893
47	+1.3503	+1.3300	+1.3633	+0.0103	+1.4000	+1.4000
48	+1.3514	+1.3267	+1.3633	+0.0131	+1.4000	+1.4000
49	+1.0989	-0.1393	+1.3700	+0.5511	+1.1514	+0.4493
50	+1.3475	+1.3233	+1.3633	+0.0140	+1.4000	+1.4000

# TNG Chart Screen



# TNG Network Animation Screen

The screenshot displays the TNG Lab software interface. The title bar reads "TNG Lab - C:\tng\fig9.tng". The menu bar includes "File", "Edit", "View", and "Help". Below the menu bar, there are two progress indicators: "50/50 gens" and "150/150 cycles", each with a corresponding bar of 20 segments. To the right of these indicators are three buttons: "Run", "Pause", and "End". Below the progress indicators is a tabbed interface with tabs for "Settings", "Results", "Chart", "Animation", and "Physics". The "Animation" tab is currently selected. The main display area shows a network diagram on a black background. The nodes are labeled with cyan text: B<sub>1</sub> through B<sub>12</sub>. The edges are labeled with yellow text: S<sub>1</sub> through S<sub>12</sub>. The network structure is as follows:

- Top row: B<sub>9</sub>, S<sub>3</sub>, B<sub>2</sub>, S<sub>6</sub>, B<sub>10</sub>, B<sub>3</sub>
- Second row: B<sub>7</sub>, S<sub>1</sub>, B<sub>6</sub>, S<sub>7</sub>, S<sub>9</sub>
- Third row: B<sub>12</sub>, B<sub>1</sub>
- Fourth row: S<sub>4</sub>, S<sub>8</sub>, B<sub>4</sub>, S<sub>11</sub>, B<sub>11</sub>, S<sub>2</sub>
- Bottom row: S<sub>12</sub>, B<sub>5</sub>, B<sub>4</sub>, S<sub>11</sub>, S<sub>10</sub>, S<sub>5</sub>, B<sub>8</sub>

Connections between nodes are shown as white lines. The network consists of several interconnected components: a top horizontal chain (B<sub>9</sub>-S<sub>3</sub>-B<sub>2</sub>-S<sub>6</sub>-B<sub>10</sub>), a central structure (S<sub>1</sub>-B<sub>6</sub>-S<sub>7</sub>), a vertical chain on the right (S<sub>9</sub>-B<sub>1</sub>), a bottom horizontal chain (S<sub>4</sub>-B<sub>5</sub>-B<sub>4</sub>-S<sub>11</sub>-S<sub>10</sub>-S<sub>5</sub>-B<sub>8</sub>), and a diagonal structure (S<sub>8</sub>-B<sub>4</sub>-B<sub>11</sub>-S<sub>2</sub>). There are also connections between B<sub>12</sub> and B<sub>5</sub>, and between B<sub>7</sub> and B<sub>6</sub>.

# TNG Physics Screen

The screenshot shows a software window titled "TNG Lab - C:\tng\fig3-7.tng". The interface includes a menu bar (File, Edit, View, Help) and a toolbar with "Run", "Pause", and "End" buttons. Two progress bars are visible: "50/50 gens" and "150/150 cycles", both fully filled. An "Animation: Stop" button is also present. Below the progress bars are tabs for "Settings", "Results", "Chart", "Animation", and "Physics". The "Physics" tab is active and contains several sub-sections:

- Physics**
  - Springs**

	Length:	Strength:
Latched	150	200
Recurrent	250	100
  - Repulsion**

Boundary	100
Trader	200
  - Friction**

Friction	0.25
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- Network Settings**

Frequency Threshold:	
Latched	6
Transient	6
- Reset** button

# In Conclusion: ACE as a Research/Teaching Tool

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- ★ ACE permits the **systematic experimental study** of decentralized market processes (descriptive, normative, qualitative...)
- ★ ACE computational laboratories facilitate and encourage **creative exploration and discovery**.
- ★ Researchers/students can test interesting hypotheses of their own devising, with immediate feedback and no original programming required.
- ★ Modular form of software permits **relatively easy modification/extension of model features**.

# Resource Sites for ACE Research Areas

<http://www.econ.iastate.edu/tesfatsi/aapplic.htm>

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- \* Embodied cognition
- \* Network formation
- \* Evolution of norms
- \* Specific market case studies
- \* Industrial organization
- \* Market design
- \* Multiple-market modelling
- \* Automated markets and software agents
- \* Development of computational laboratories
- \* Parallel experiments (real and computational agents)
- \* Empirical validation
- \* Many others...