

APPENDIX: THE LOG-LIKELIHOOD FUNCTION FOR KUHN-TUCKER MODEL

The purpose of this appendix is to provide the interested reader with the details of the log-likelihood function used in the empirical section of the manuscript. The log-likelihood function below is specific to a Kuhn Tucker Model given four choice alternatives and errors drawn from a GEV distribution with correlation between alternatives (1,2) and (3,4). The contribution to the log-likelihood function for an individual who chooses consumption pattern ω is given by:

$$\begin{aligned}
 \ln L = & -\sum_{j=1}^2 \frac{d_j g_j}{\mu \theta^S} - \sum_{j=3}^4 \frac{d_j g_j}{\mu \theta^N} \\
 & - \left[\exp\left(\frac{-g_1}{\mu \theta^S}\right) + \exp\left(\frac{-g_2}{\mu \theta^S}\right) \right]^{\theta^S} - \left[\exp\left(\frac{-g_3}{\mu \theta^N}\right) + \exp\left(\frac{-g_4}{\mu \theta^N}\right) \right]^{\theta^N} \\
 & + (d_1 + d_2)(\theta^S - 1) \log \left[\exp\left(\frac{-g_1}{\mu \theta^S}\right) + \exp\left(\frac{-g_2}{\mu \theta^S}\right) \right] \\
 & + (d_3 + d_4)(\theta^N - 1) \log \left[\exp\left(\frac{-g_3}{\mu \theta^N}\right) + \exp\left(\frac{-g_4}{\mu \theta^N}\right) \right] \\
 & + (d_1 d_2) \log \left(1 - \frac{\theta^S - 1}{\theta^S} \left[\exp\left(\frac{-g_1}{\mu \theta^S}\right) + \exp\left(\frac{-g_2}{\mu \theta^S}\right) \right] \right)^{-\theta^S} \\
 & + (d_3 d_4) \log \left(1 - \frac{\theta^N - 1}{\theta^N} \left[\exp\left(\frac{-g_3}{\mu \theta^N}\right) + \exp\left(\frac{-g_4}{\mu \theta^N}\right) \right] \right)^{-\theta^N} \\
 & + \log |J_\omega| + (d_1 + d_2 + d_3 + d_4) \log(\mu),
 \end{aligned} \tag{A1}$$

where

$$d_i = \begin{cases} 1 & x_i > 0 \\ 0 & \text{otherwise} \end{cases}$$

The Jacobian transformation terms in equation (A1) are given by:

$$J_\omega = F_j \text{ for } \omega = \{j\}, j = 1,2,3,4. \tag{A2}$$

$$J_\omega = \prod_{j \in \omega} F_j - \prod_{j \in \omega} z_j \text{ for } \omega = \{1,2\}, \{1,3\}, \{1,4\}, \{2,3\}, \{2,4\}, \text{ and } \{3,4\}. \tag{A3}$$

$$J_\omega = \prod_{j \in \omega} F_j + 2 \prod_{j \in \omega} z_j - \sum_{j \in \omega} F_j \left(\prod_{\substack{k \in \omega \\ k \neq j}} z_k \right) \text{ for } \omega = \{1,2,3\}, \{1,2,4\}, \{1,3,4\}, \text{ and } \{2,3,4\}. \quad (\text{A4})$$

and

$$J_\omega = F_1 F_2 F_3 F_4 - 3z_1 z_2 z_3 z_4 + 2(F_1 z_2 z_3 z_4 + F_2 z_1 z_3 z_4 + F_3 z_1 z_2 z_4 + F_4 z_1 z_2 z_3) - (F_1 F_2 z_3 z_4 + F_1 F_3 z_2 z_4 + F_1 F_4 z_2 z_3 + F_2 F_3 z_1 z_4 + F_2 F_4 z_1 z_3 + F_3 F_4 z_1 z_2) \text{ for } \omega = \{1,2,3,4\} \quad (\text{A5})$$

where

$$z_j \equiv \frac{p_j}{y - \sum_{k=1}^4 p_k x_k} = \frac{\partial \mathcal{E}_k}{\partial x_j} \quad \forall k \neq j, \quad (\text{A6})$$

$$F_j \equiv \frac{1}{x_j + \theta} + z_j = \frac{\partial \mathcal{E}_j}{\partial x_j} \quad \forall j, \quad (\text{A7})$$